

Weekly Review 5 0910

- 1) Evaluate each of the following limits algebraically and discuss the continuity of the function including any points of discontinuity.

a) $\lim_{x \rightarrow 0} \frac{5x^3 + 8x^2}{3x^4 - 16x^2}$

b) $\lim_{x \rightarrow 0} (\csc x - \cot x)$

- 2) Find $\frac{dy}{dx}$ and the slope of the tangent line at (2, 3).

a) $x^2 + y^2 = 2y^3$

b) $xy^2 - y^3 = x^2 - 5$

- 3) Find the equation of the line tangent to the graph of $y = \sqrt{x}$ at the point on the curve where the y-coordinate is exactly one-third the value of the x-coordinate given $x > 0$. Show the work that leads to your answer.

- 4) Find a value for a so that the function is continuous. Does this choice for a also make the function differentiable? If so, explain, if not, find a value for a that will make the function differentiable at all points.

$$f(x) = \begin{cases} 4 - x^2, & x < -1 \\ ax^2 - 1, & x \geq -1 \end{cases}$$

- 5) Use composition and the chain rule to show $\frac{dy}{dx} = 6t \sin^2(t^2 + 5) \cos(t^2 + 5)$ if $y = [\sin(t^2 + 5)]^3$. This is an example where you may have three factors involved in the process.

Answers to Weekly Review 5

1)

a) $-\frac{1}{2}$

b) 0

2)

a) $\frac{dy}{dx} = \frac{2x}{6y^2 - 2y}$, $\left. \frac{dy}{dx} \right|_{(2,3)} = \frac{1}{12}$

b) $\frac{dy}{dx} = \frac{2x - y^2}{2xy - 3y^2}$, $\left. \frac{dy}{dx} \right|_{(2,3)} = \frac{1}{3}$

3) Tangent line: $y = \frac{1}{6}(x - 9) + 3$

4) When $a = 4$ the function is continuous, when $a = -1$ the derivatives would be equal, but because the function would not be continuous when $a = -1$, we can't talk about the function being differentiable at that point.

5) Answers will vary